For GSP5

The slope-intercept form of a line, y = mx + b, is one of the best-known formulas in algebra. In this activity you'll learn about this equation first by exploring one line, and then by exploring whole *families* of lines.

SKETCH AND INVESTIGATE

Choose Graph | Define Coordinate System. To hide the points, select them and choose Display | Hide Points.

Choose **Graph** | **Plot Points.** Enter the coordinates in the Plot Points dialog box, click **Plot;** then click **Done.**

To measure the coordinates, choose **Measure** | **Coordinates.**

If *m* is a decimal such as 1.5, write it as a fraction such as 3/2. If it's a whole number such as 3, write it as a fraction such as 3/1.

- You'll start this activity with m = 2 and b = 1 as you explore the line y = 2x + 1.
 - 1. In a new sketch, define a coordinate system and hide the points (0, 0) and (1, 0).
- **Q1** For y = 2x + 1, what is y when x = 0? Write your answer as an ordered pair.
- 2. Plot this point. Why does it make sense to call this point the *y-intercept*?
- **Q2** You found that the *y*-intercept of y = 2x + 1 is 1. What is the *y*-intercept of y = 3x + 7? Explain why the *y*-intercept of y = mx + b is always *b*.

You've learned that *slope* can be written as *rise/run*. The slope of the line y = 2x + 1 is 2, which you can think of as 2/1 (*rise* = 2 and *run* = 1).

- Translate your plotted point using this slope. Choose Transform | Translate, use a rectangular translation vector, and enter 1 for the run (horizontal) and 2 for the rise (vertical).
- **Q3** What are the coordinates of the new point? Substitute them into y = 2x + 1 to show they satisfy the equation.
- **Q4** Translate the new point by the same *rise* and *run* values to get a third point. Find the coordinates of this third point, and verify that it satisfies the equation y = 2x + 1.

Translate 🗶
Translation Vector: Polar In Rectangular Marked
Horizontal:
1.0 cm
Vertical:
2.0 cm
Help Cancel Translate

4. Select any two of the three points you've plotted, and choose Construct | Line.

What you've done so far is one technique for plotting lines in the form y = mx + b:

- Plot the *y*-intercept (0, *b*).
- Rewrite *m* as *rise/run* (if necessary).
- Find a second point by translating the *y*-intercept by *rise* and *run*.
- Connect the points to get the line. Plot a third point to check the line.
- **Q5** Using the method just described, plot these lines on graph paper.

a. $y = 3x - 2$	b. $y = (2/3)x + 2$
c. $y = -2x + 1$	d. $y = 2.5x - 3$



EXPLORING FAMILIES OF LINES

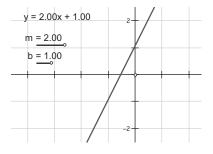
Now that you've plotted a line, focus on how *m* and *b* affect the equation.

5. Open Slope Intercept.gsp.

The graph of y = 2x + 1 is already plotted. You can change *m* and *b* by adjusting their sliders.

To adjust a slider, drag the point at its tip.

To erase traces left by the line, choose **Display | Erase Traces.** **Q6** Adjust slider *m* and observe the effect. Describe the differences between lines with m > 0, m < 0, and m = 0. What happens to the line as *m* becomes increasingly positive? Increasingly negative?



- **Q7** Now adjust slider *b*. Describe the effect this value has on the line.
- 6. Select the line and choose **Display** | **Trace Line**.
- **Q8** Adjust *m* and observe the trace pattern that forms. Describe the lines that appear when you change *m*. What do they have in common?
- **Q9** Erase the traces and adjust *b*. How would you describe the lines that form when you change *b*? What do they have in common?
- 7. Turn off tracing by selecting the line and choosing **Display** | **Trace Line** again. Erase any remaining traces.
- **Q10** For each description below, write the equation in slope-intercept form. To check your equation, adjust *m* and *b* so that the line appears on the screen.
 - a. slope is 2.0; *y*-intercept is (0, -3)
 - b. slope is -1.5; *y*-intercept is (0, 4)
 - c. slope is 3.0; *x*-intercept is (-2, 0)
 - d. slope is -0.4; contains the point (-6, 2)
 - e. contains the points (3, 5) and (-1, 3)

EXPLORE MORE

- **Q11** Attempt to construct a line through the points (3, 0) and (3, -3) by adjusting the sliders in the sketch. Explain why this is impossible. (Why can't you write its equation in slope-intercept form?)
- **Q12** Can you construct the same line with two different slider configurations? If so, provide two different equations for the same line. If not, explain why.