The slope-intercept form of a line, $y=m x+b$, is one of the best-known formulas in algebra. In this activity you'll learn about this equation first by exploring one line, and then by exploring whole families of lines.

## SKETCH AND INVESTIGATE

Choose Graph | Define Coordinate System. To hide the points, select them and choose Display | Hide Points.

Choose Graph | Plot Points. Enter the coordinates in the Plot Points dialog box, click Plot; then click Done.

To measure the coordinates, choose Measure | Coordinates.

If $m$ is a decimal such as 1.5 , write it as a fraction such as $3 / 2$. If it's a whole number such as 3 , write it as a fraction such as $3 / 1$.

You'll start this activity with $m=2$ and $b=1$ as you explore the line $y=2 x+1$.

1. In a new sketch, define a coordinate system and hide the points $(0,0)$ and $(1,0)$.

Q1 For $y=2 x+1$, what is $y$ when $x=0$ ? Write your answer as an ordered pair.
2. Plot this point. Why does it make sense to call this point the $y$-intercept?

Q2 You found that the $y$-intercept of $y=2 x+1$ is 1 . What is the $y$-intercept of $y=3 x+7$ ? Explain why the $y$-intercept of $y=m x+b$ is always $b$.

You've learned that slope can be written as rise/run. The slope of the line $y=2 x+1$ is 2 , which you can think of as $2 / 1($ rise $=2$ and run $=1)$.
3. Translate your plotted point using this slope. Choose Transform | Translate, use a rectangular translation vector, and enter 1 for the run (horizontal) and 2 for the rise (vertical).

Q3 What are the coordinates of the new point? Substitute them into $y=2 x+1$ to show they satisfy the equation.

Q4 Translate the new point by the same rise and run values to get a third point. Find the
 coordinates of this third point, and verify that it satisfies the equation $y=2 x+1$.
4. Select any two of the three points you've plotted, and choose Construct | Line.

What you've done so far is one technique for plotting lines in the form $y=m x+b$ :

- Plot the $y$-intercept $(0, b)$.
- Rewrite $m$ as rise/run (if necessary).
- Find a second point by translating the $y$-intercept by rise and run.
- Connect the points to get the line. Plot a third point to check the line.

Q5 Using the method just described, plot these lines on graph paper.
a. $y=3 x-2$
b. $y=(2 / 3) x+2$
c. $y=-2 x+1$
d. $y=2.5 x-3$

## EXPLORING FAMILIES OF LINES

Now that you've plotted a line, focus on how $m$ and $b$ affect the equation.

## 5. Open Slope Intercept.gsp.

The graph of $y=2 x+1$ is already plotted. You can change $m$ and $b$ by adjusting their sliders.

To adjust a slider, drag the point at its tip.

Q6 Adjust slider $m$ and observe the effect.
Describe the differences between lines with $m>0, m<0$, and $m=0$. What happens to
 the line as $m$ becomes increasingly positive? Increasingly negative?

Q7 Now adjust slider $b$. Describe the effect this value has on the line.
6. Select the line and choose Display | Trace Line.

08 Adjust $m$ and observe the trace pattern that forms. Describe the lines that appear when you change $m$. What do they have in common?

To erase traces left by the line, choose Display |Erase Traces.

09 Erase the traces and adjust $b$. How would you describe the lines that form when you change $b$ ? What do they have in common?
7. Turn off tracing by selecting the line and choosing Display | Trace Line again. Erase any remaining traces.

Q10 For each description below, write the equation in slope-intercept form. To check your equation, adjust $m$ and $b$ so that the line appears on the screen.
a. slope is $2.0 ; y$-intercept is $(0,-3)$
b. slope is $-1.5 ; y$-intercept is $(0,4)$
c. slope is $3.0 ; x$-intercept is $(-2,0)$
d. slope is -0.4 ; contains the point $(-6,2)$
e. contains the points $(3,5)$ and $(-1,3)$

## EXPLORE MORE

Q11 Attempt to construct a line through the points $(3,0)$ and $(3,-3)$ by adjusting the sliders in the sketch. Explain why this is impossible. (Why can't you write its equation in slope-intercept form?)

Q12 Can you construct the same line with two different slider configurations? If so, provide two different equations for the same line. If not, explain why.

